

Reduction for nutation — rigorous formulae

Nutations in longitude ($\Delta\psi$) and in obliquity ($\Delta\epsilon$) together with the true obliquity of the ecliptic (ϵ) for 2006 have been calculated using the IAU 2000A series, and are tabulated on pages B32–B39. A mean place (\mathbf{r}_m) may be transformed to a true place (\mathbf{r}_t), and vice versa, as follows:

$$\mathbf{r}_t = \mathbf{N} \mathbf{r}_m \quad \mathbf{r}_m = \mathbf{N}^{-1} \mathbf{r}_t = \mathbf{N}' \mathbf{r}_t$$

$$\text{where} \quad \mathbf{N} = \mathbf{R}_1(-\epsilon) \mathbf{R}_3(-\Delta\psi) \mathbf{R}_1(+\epsilon_A)$$

$\epsilon = \epsilon_A + \Delta\epsilon$, and ϵ_A is given at the top of page B29. The matrix for nutation is given by

$$\mathbf{N} = \begin{pmatrix} \cos \Delta\psi & -\sin \Delta\psi \cos \epsilon_A & -\sin \Delta\psi \sin \epsilon_A \\ \sin \Delta\psi \cos \epsilon & \cos \Delta\psi \cos \epsilon_A \cos \epsilon + \sin \epsilon_A \sin \epsilon & \cos \Delta\psi \sin \epsilon_A \cos \epsilon - \cos \epsilon_A \sin \epsilon \\ \sin \Delta\psi \sin \epsilon & \cos \Delta\psi \cos \epsilon_A \sin \epsilon - \sin \epsilon_A \cos \epsilon & \cos \Delta\psi \sin \epsilon_A \sin \epsilon + \cos \epsilon_A \cos \epsilon \end{pmatrix}$$